

## PROJECT METHOD FOR WEIGHING ELECTRODYNAMIC CELLS

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**Abstract:** This article comprise in the authors research and realization same high performed devices for weighing, forces and mass, which may resolved more exacting applications of different domain: medical electronic- human dynamic equilibrium study and human gait human analysis, electronic devices for measure and control weighing, mass and force.

**Keywords:** *electrodynamics cells, medical electronic, measure weighing mass and force, measurement process, solenation elements, magnetic field, harmonic variation.*

### I. INTRODUCTION

The project of an electrodynamic transducers have in view the dimensioning of the main active solenation elements, in direct current, respectively in alternative current, the dimensioning of magnetic circuits starting from the necessity to achieve the imposed performances according to some conditions given by the loading cooling of the coil, as well as the execution technology, and the operation of electrodynamic transducers [13]. The project is achieved in the following hypotheses – the modulation of the constant magnetic field in the working air gap by the magnetic field of the coil in AC is neglected the time variable quantities are considered with harmonic variation, - the project algorithm is draw up in hypothesis of using computer.

### II. PROGRAMMING METHOD FOR WEIGHING ELECTRODYNAMICS CELLS

Programming elements of the electrodynamic vibrator are show in figure 1.

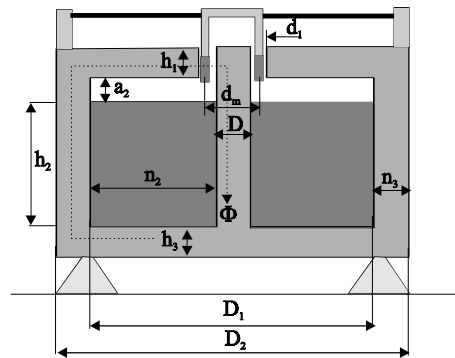


figure 1

The loading coefficient in current is  $K_0 = \theta_2 / \theta_1$  where  $\theta_1$  and  $\theta_2$  are the solenation in DC current, respectively, alternative current, and it has an optimal value  $K_0 = 6$  (it resulted from the projecting analyses done by other specialised firms [4-13]). The force amplitude developed by the transducer is:

$$F_o = \sqrt{2} B_o I_S W_1 I_m = \sqrt{2} \pi B_o D \theta_1 \quad \text{where:}$$

$F_o$  is the force that the amplitude developed in N, its value being given by the programming theme,  $B_o$  represent the magnetic induction from the air gap in T,  $I_S$  is represent the effective value of the AC current in the mobile coil in A,  $W_1$  is number of whirls of the coil of AC current,  $I_m$  represent the

medium length of the whirl,  $I_m=2\pi d_m$ , in the calculation there will be taken,  $I_m=\pi D$ , in this way there results a higher solenation, therefore the calculation will be covering, D represent the diameter of central core,  $\theta_1$  the solenation of the coil AC current in Asp. From the condition of thermic stability, considering the coil of AC current bilaterally cooled by conversion, in result [1,2][12,13]:

$$\tau = \frac{\rho_1 \theta_1^2}{2\alpha_1 f_1 n_1 h_1^2} \leq \tau_{1a} \text{ where:}$$

$\rho_1 = \rho_0(1+\alpha\pi_{1a})$  represent the resistivity of the coil conductor in hot state,  $\alpha$  the coefficient of the resistivity variation with the temperature ( $\alpha=0.004^\circ C^{-1}$  for the copper conductor),  $T_1$  the supertemperature of the coil of Ac current in  $^\circ C$ ,  $\pi_{1a}$  the permitted supertemperature of the coil of AC current ( $\pi_{1a}=100^\circ C$  for a copper conductor CuEm type ET 155),  $\alpha_1$  the coefficient of the heat transmission at the mobile coil surface, for natural coding being determined by measurement,  $\alpha_1=20W/m^2K$ ,  $f_1=0,4;\dots,0,6$  with superior values for higher transducers (with higher developed force),  $n_1$  the mobile coil thickness in m,  $h_1$  the mobile coil leigh in m. The solenation in DC current is obtain by applying the magnetic circuit law for a contour made up by a field main line:

$$\Phi H dl = H_0 \delta + H_{fe} I_{fe} = \theta_2 = K_{fe} H_0 \delta$$

where:  $\delta$  in the length of the air gap in m,  $H_{fe}$ ,  $H_0$  - the magnetic field intensity in iron, respectively, in the air gap  $K_{fe} = (\theta_0 + \theta_{fe})/\theta_0$  - the coefficient of the calculation for the magnetic voltage drop on the iron section,  $\theta_0, \theta_{fe}$  the corresponding solenation for the magnetization of the air gap, respectively of the iron from the magnetic circuits,  $K_{fe}=1,1\dots,1,4$  (in the primary programming phase,  $H_{fe} I_{fe}$  are not know, which is taken into consideration through  $K_{fe}$ ).

In order to obtain an induction in drawn up by programming that in the neighborhood of the air gap should exist a very high induction (close the saturation induction of material in the rest of the magnetic circuit, a low induction, in order to reduce the magnetic voltage drop in iron). For this reason, the minimal section of a iron portion is taken in the imminent neighborhood of the air gap, on the inferior magnetic flux transmission to the polar part and to the air gap. The section of the inferior magnetic yoke plate  $S_3$ , in order to reduce the magnetic voltage drop in iron, is taken:  $S_0=S_{fe}=Dh_1$ ,  $S_{fe}=K_1 S_0=S_{fe}$ ,  $S_3=K_1 S_0$ ,  $K_1 \pi D h_1 = \pi D h_3$ ,  $h_3=K_1 h_1$  where:  $h_3$  represent the high of the growth coefficient of the section in iron, determined by the optimization calculations  $K_1=1,1\dots,1,4$ . Analogously with relation:

$$\tau = \frac{\rho_1 \theta_1^2}{2\alpha_1 f_1 n_1 h_1^2} \leq \tau_{1a} \text{ it is obtain for the coil DC current (which we consider as having an iron care):}$$

$$\tau_2 = \frac{\rho_2 \theta_2^2}{2\alpha_2 f_2 n_2 h_2^2} \leq \tau_{2a}$$

where:  $\alpha_1=10W/m^2K$  the heat transmission coefficient to surface of the DC current coil,  $f_2$  the filling coefficient of the coil of the DC current,  $f_2=0,4\dots,0,6$ , the high values are taken for big coils and those having no insulation between their layers,  $n_2$  the thickness of the DC current coil in m,  $h_2$  the leight of DC current coil. The inferior diameter of the magnetic lateral yoke plare  $D_1=D+2n_2$ . From the law of magnetic flux relation results:

$$\frac{\pi D_2}{4} = \frac{\pi(D_2^2 - D_1^2)}{4}$$

$$K_1(\pi D h_1) = \frac{\pi D^2}{4}$$

In the programming of the electrodynamic transducer we have also in view the coefficients of a geometric shape K, Kn and the coefficients of a security  $K_2$ ,  $K_{f1}=h_1/n_1$  the shape coefficient of the coil of alternative current,  $K_{f1}=5\dots,7$ ,  $K_2=a_2/h_1$  the coefficient of security in order to avoid the hitting of the mobile coil against that of DC current  $K_2=0,4\dots,0,6$ . By Rotters' relation, we calculate the different portions permeances of the air gap, the permeance corresponding to the flux around the air gap. If the magnetic voltage drop on the air gap is written down in two different ways (referring to the total flux, respectively to the useful flux) there will be obtain:

$$\Delta_u = \frac{2\pi\mu_0 h_1}{\ln\left(1 + \frac{2\delta}{D}\right)}$$

$$\Delta_s = \mu_0 D \left[ 3 + 2 \ln\left(\frac{a_2}{2\delta} + \frac{1}{2}\right) + \ln\left(1 + \frac{D}{\delta}\right) \right]$$

$$\frac{\Phi}{\Delta_0} = \frac{\Phi_U}{\Delta_U}$$

where:  $\Phi$  represent the total flux,  $\Phi_U$  is useful flux in the air gap,  $\Delta_0$  is the total permeance of the air and U represent the air gap permeance. The coefficient of magnetic circuit dispersion  $K_0$  is:

$$K_\theta = \frac{\Phi}{\Phi_U} = \frac{\Delta_0}{\Delta_U} = 1 + \frac{\Delta_s}{\Delta_U}$$

$$K_\theta = 1 + \frac{D \ln\left(1 + \frac{2\delta}{D}\right)}{2\pi h_1} \cdot \left[ 3 + 2 \ln\left(\frac{a_2}{\delta}\right) + \ln\left(1 + \frac{D}{\delta}\right) \right]$$

from the magnetic flux retention low results:

$$\Phi = K_\theta \Phi_U$$

$$B_{Fe} S_{Fe} = K_\theta B_0 S_0$$

$$B_{Fe} S_0 K_1 = K_\theta B_0 S_0$$

$$B_{Fe} = \frac{K_{\theta} B_0}{K_1}$$

The  $B_0$  induction in the air gap is imposed by the researching theme. The magnetic field intensity in iron  $H_{fe}=H_{fe}(B_{fe})$  is obtain from the magnetization characteristics for the calculated value of the induction by the relation. For the result geometric configuration is calculated coefficient  $K$ :

$$K'_{Fe} = 1 + \frac{\mu_0 H_{Fe} l_{Fe}}{B_0 S}$$

$$l_{Fe} = 2 \left( n_2 + \frac{n_3}{2} + \frac{D}{6} + h_2 + a_2 + \frac{h_1}{2} + \frac{h_3}{2} \right) - \delta$$

The  $K_{fe}$  value is compared to that initially imposed  $K_{fe}$ , where is determined the calculation error in its estimation. If imposed:

$$\varepsilon_{KFe} = \left| \frac{K'_{Fe} - K_{Fe}}{K'_{Fe}} \right| = \left| 1 - \frac{K_{Fe}}{K'_{Fe}} \right| \leq \varepsilon_{Ke}$$

The preliminary calculation is framed into the initially imposed data, if imposed  $\varepsilon_{Kfe} \leq \varepsilon_{Ke}$  the calculations with the new value  $K_2$  are resumed:

The iron mass  $m_{fe}$ :

$$m_{Fe} = \rho_{Fe} \left[ 2\pi D_2 H + \frac{\pi(D_1^2 - D^2)}{4} (h_3 + h_1) \right]$$

$$H = h_1 + h_2 + h_3 + a_2$$

The copper  $m_{Cu}$ :

$$m_{Cu} \approx \rho_{Cu} f_2 \frac{\pi(D_1^2 - D^2)h_2}{4}$$

The auxiliary elements mass  $m_{aux}=K_3(m_{fe}+m_{Cu})$  with  $K_3=0,05\dots 0,2$ . The total mass of the transducer:

$$m_T = m_{aux} + m_{Cu} + m_{Fe}$$

### III. THE EQUATIONS WHICH DESCRIBE THE OPERATION OF AN ELECTRODYNAMIC TRANSDUCER [13].

If we write down the equilibrium equation at the terminal jack of the mobile coil in voltage:

$$u = Ri + Li + Bl \left( \frac{dx_m}{dt} + \frac{dx_S}{dt} \right) \text{ where:}$$

$R$  – resistance,  $L$ -inductance of the mobile coil,  $B$ - the magnetic induction in the air gap,  $l$ - the length of the coil conductor,  $dx_m/dt$  – the linear speed of the mobile equipment,  $dx_S$  - the speed of stator and the supply voltage of the mobile coil The equation of a mechanical equilibrium is:

$$M \left( \frac{d^2 x_m}{dt^2} - \frac{d^2 x_S}{dt^2} \right) + C \left( \frac{dx_m}{dt} - \frac{dx_S}{dt} \right) + K_e (x_m - x_S) = F$$

where:  $M$  – the total mass in displacement,  $C$ - the coefficient of the dynamic viscosity,  $K_e$ - the

equivalent coefficient of elasticity an  $F$  – force developed by the transducer:

$$F = B L i = \Gamma i$$

If voltage has harmonic variation the current and its displacement has also some harmonic variations. Writing down in a simplified complex the relations of stationary condition, we have:

$$\underline{U} = \underline{Z}_e \cdot \underline{I} + \Gamma (\underline{V}_m - \underline{V}_M)$$

$$\underline{Z}_M \underline{V}_M + \underline{Z}_e (\underline{V}_m - \underline{V}_M) = \underline{F}$$

$$\underline{Z}_m \underline{V}_m + \underline{Z}_e (\underline{V}_m - \underline{V}_M) = -\underline{F}$$

$$\underline{F} = \Gamma \underline{I}$$

where:  $\underline{Z}_M = j\omega M_M$  represent the mechanical impedance of the elastic element, the previous system and  $\underline{Z}_m = j\omega m$  represent the mechanical impedance of the mobil element. If we note:  $\underline{Z}_e = C_e + k_e / j\omega$  the mechanical impedance of the elastic element the previous system becomes:

$$\underline{U} = R \cdot \underline{I} + L \cdot \underline{I} + \Gamma \dot{\underline{I}}$$

$$M \cdot \ddot{x} + C \cdot \dot{x} + K_e x - \Gamma \cdot I = 0$$

In the harmonic stationary condition we can write down in a simplified complex:

$$\underline{x} = X e^{j\alpha}$$

$$\underline{U} = U e^{j\alpha}$$

$$\underline{i} = I e^{j\alpha}$$

By replacing into the relation that characterize the system we obtain:

$$(R + j\omega L)I + j\omega \Gamma X = U$$

$$-(K_e - M\omega^2 + j\omega C)X = 0$$

$$\underline{I} = \frac{U - j\omega \Gamma X}{R + j\omega L}$$

$$\Gamma \frac{U - j\omega \Gamma X}{R + j\omega L} - (K_e - M\omega^2 + j\omega C)X = 0$$

or:

$$\underline{X} = \frac{\Gamma U}{(K_e - M\omega^2 + j\omega C)(R + j\omega L) + j\omega \Gamma^2}$$

$$\underline{I} = \frac{\underline{U}}{R + j\omega L + j\omega \frac{\Gamma}{K_e - M\omega^2 + j\omega C}}$$

The force developed by the transducer will be defined by relation:

$$\underline{F} = \underline{\Gamma I} = \frac{\underline{\Gamma U}}{R + j\omega L + j\omega \frac{\Gamma^2}{K_e - M\omega^2 + j\omega C}}$$

$$\Gamma = B \cdot L$$

If voltage source has a constant amplitude, the force produced by the transducer is function of the frequency, the relation being of reverse proportionality, with a considerable diminution of the force in the area the resonance frequency of the excited system. During the rest, the impedance of coil  $Z_L = R + j\omega L$ , is powerfully resistive ( $L=0$ ) an the last relation above becomes:

$$\underline{F} = \underline{\Gamma I} = \frac{\underline{\Gamma U}}{R + j\omega \frac{\Gamma^2}{K_e - M\omega^2 + j\omega C}}$$

#### IV. CONCLUSIONS

1) In order that the force produced by the transducer should take minimal values st the resistance, the ratio  $R/\Gamma$  must be as high as possible (R-high,  $\Gamma$ - low).

2) It is necessary the introduction of some compensatory circuits of the coil inductivity through series compensation with capacitors and the avoidance of the operation at resonance through the practicing of a short circuit whirl in the working air gap. Recommended for the achievement of the whirl compensation in the short circuit is the one of a closed magnetic screen type which encloses the mobile coil, and on the main pole we place a cooper ring with a thickness of 1...2mm and the high of the working air gap.

3) The achievement of the mobile coil from two section, with the same number of whirls winded in opposite ways and connected in series, in this case, the coil equal as value and it superposes as direction, but the proper magnetic flux of the concatenation of the each section is opposite, canceling each other, fact that leads to the diminution of the mobile coil reactance.

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